# TI-83/84 Guide for Introductory Statistics 

Includes step-by-step instructions, practice exercises, and links to video tutorials. Covers all calculator features needed for $A P{ }^{\circledR}$ Statistics Exam

> Instructions excerpted from Advanced High School Statistics, 3rd ed. available for FREE at openintro.org/ahss

Leah Dorazio<br>San Francisco University High School<br>leah@openintro.org

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## Summarizing data

## Entering data

## ㅇ․ TI-83/84: ENTERING DATA

The first step in summarizing data or making a graph is to enter the data set into a list. Use STAT, Edit.

1. Press STAT.
2. Choose 1:Edit.
3. Enter data into L1 or another list.

## Calculating summary statistics

## ㅇ․ TI-84: CALCULATING SUMMARY STATISTICS

Use the STAT, CALC, 1-Var Stats command to find summary statistics such as mean, standard deviation, and quartiles.

1. Enter the data as described previously.
2. Press STAT.
3. Right arrow to CALC.
4. Choose 1:1-Var Stats.
5. Enter L1 (i.e. 2ND 1) for List. If the data is in a list other than L1, type the name of that list.
6. Leave FreqList blank.
7. Choose Calculate and hit ENTER.

TI-83: Do steps 1-4, then type L1 (i.e. 2nd 1) or the list's name and hit ENTER.

Calculating the summary statistics will return the following information. It will be necessary to hit the down arrow to see all of the summary statistics.

| $\bar{x}$ | Mean | $n$ | Sample size or \# of data points |
| :--- | :--- | :--- | :--- |
| $\sum \mathrm{x}$ | Sum of all the data values | $\operatorname{minX}$ | Minimum |
| $\sum \mathrm{x}^{2}$ | Sum of all the squared data values | $\mathrm{Q}_{1}$ | First quartile |
| SX | Sample standard deviation | Med | Median |
| $\sigma \mathrm{x}$ | Population standard deviation | maxX | Maximum |

## Drawing a box plot

ํ. TI-83/84: DRAWING A BOX PLOT

1. Enter the data to be graphed as described previously.
2. Hit $2 N D$ Y = (i.e. STAT PLOT).
3. Hit enter (to choose the first plot).
4. Hit Enter to choose ON.
5. Down arrow and then right arrow three times to select box plot with outliers.
6. Down arrow again and make Xlist: L1 and Freq: 1.
7. Choose ZOOM and then 9 :ZoomStat to get a good viewing window.

## What to do if you cannot find L1 or another list

## TI-83/84: WHAT TO DO IF YOU CANNOT FIND L1 OR ANOTHER LIST

Restore lists L1-L6 using the following steps:

1. Press Stat.
2. Choose 5:SetUpEditor.
3. Hit Enter.

## Practice exercises

## GUIDED PRACTICE 0.1

Enter the following 10 data points into a list on a calculator:

$$
5,8,1,19,3,1,11,18,20,5
$$

Find the summary statistics and make a box plot of the data. ${ }^{1}$

## Finding area under the normal curve

## ㅇ․ TI-84: FINDING AREA UNDER THE NORMAL CURVE

Use 2ND VARS, normalcdf to find an area/proportion/probability to the left or right of a Z-score or between two Z-scores.

1. Choose 2ND VARS (i.e. DISTR).
2. Choose 2:normalcdf.
3. Enter the Z-scores that correspond to the lower (left) and upper (right) bounds.
4. Leave $\mu$ as 0 and $\sigma$ as 1 .
5. Down arrow, choose Paste, and hit ENTER.

TI-83: Do steps 1-2, then enter the lower bound and upper bound separated by a comma, e.g. normalcdf (2, 5), and hit ENTER.

[^0]

## Find a Z-score that corresponds to a percentile

## O० TI-84: FIND A Z-SCORE THAT CORRESPONDS TO A PERCENTILE

Use 2ND VARS, invNorm to find the Z-score that corresponds to a given percentile.

1. Choose 2ND vars (i.e. DISTR).
2. Choose 3:invNorm.
3. Let Area be the percentile as a decimal (the area to the left of desired Z-score).
4. Leave $\mu$ as 0 and $\sigma$ as 1 .
5. Down arrow, choose Paste, and hit ENTER.

TI-83: Do steps 1-2, then enter the percentile as a decimal, e.g. invNorm (.40), then hit Enter.

## Practice exercises

## EXAMPLE 0.2

Use a calculator to determine what percentile corresponds to a Z-score of 1.5.
Always first sketch a graph: ${ }^{2}$


To find an area under the normal curve using a calculator, first identify a lower bound and an upper bound. Theoretically, we want all of the area to the left of 1.5 , so the left endpoint should be $-\infty$. However, the area under the curve is nearly negligible when Z is smaller than -4 , so we will use -5 as the lower bound when not given a lower bound (any other negative number smaller than -5 will also work). Using a lower bound of -5 and an upper bound of 1.5 , we get $P(Z<1.5)=0.933$.

## (G)

## GUIDED PRACTICE 0.3

Find the area under the normal curve to right of $Z=2$. ${ }^{3}$

[^1]
## EXAMPLE 0.5

Use a calculator to find the Z-score that corresponds to the 40th percentile.
Letting Area be 0.40 , a calculator gives -0.253 . This means that $Z=-0.253$ corresponds to the 40 th percentile, that is, $P(Z<-0.253)=0.40$.

## GUIDED PRACTICE 0.6

Find the Z-score such that 20 percent of the area is to the right of that Z-score. ${ }^{5}$

## EXAMPLE 0.7

In a large study of birth weight of newborns, the weights of 23,419 newborn boys were recorded. ${ }^{6}$ The distribution of weights was approximately normal with a mean of 7.44 lbs ( 3376 grams) and a standard deviation of 1.33 lbs ( 603 grams). The government classifies a newborn as having low birth weight if the weight is less than 5.5 pounds. What percent of these newborns had a low birth weight?

We find an area under the normal curve between -5 (or a number smaller than -5 , e.g. -10 ) and a Z-score that we will calculate. There is no need to write calculator commands in a solution. Instead, continue to use standard statistical notation.

$$
\begin{aligned}
Z & =\frac{5.5-7.44}{1.33} \\
& =-1.49 \\
P(Z<-1.49) & =0.068
\end{aligned}
$$

Approximately $6.8 \%$ of the newborns were of low birth weight.

[^2]
## Probability and probability distributions

Computing the binomial coefficient

## ㅇ. TI-83/84: COMPUTING THE BINOMIAL COEFFICIENT, $\binom{n}{k}$

Use MATH, PRB, nCr to evaluate $n$ choose $r$. Here $r$ and $k$ are different letters for the same quantity.

1. Type the value of $n$.
2. Select MATH.
3. Right arrow to PRB.
4. Choose 3:nCr.
5. Type the value of k .
6. Hit Enter.

Example: 5 nCr 3 means 5 choose 3.

## Computing the binomial formula

ㅇ․ TI-84: COMPUTING THE BINOMIAL FORMULA, $P(X=k)=\binom{n}{k} p^{k}(1-p)^{n-k}$
Use 2ND VARS, binompdf to evaluate the probability of exactly $k$ occurrences out of $n$ independent trials of an event with probability $p$.

1. Select 2ND VARS (i.e. DISTR)
2. Choose $\mathrm{A}:$ binompdf (use the down arrow).
3. Let trials be $n$.
4. Let p be $p$
5. Let x value be $k$.
6. Select Paste and hit Enter.

TI-83: Do steps 1-2, then enter $n, p$, and $k$ separated by commas: binompdf ( $\mathrm{n}, \mathrm{p}, \mathrm{k}$ ). Then hit Enter.

## Computing a cumulative binomial probability

TI-84: COMPUTING $P(X \leq k)=\binom{n}{0} p^{0}(1-p)^{n-0}+\ldots+\binom{n}{k} p^{k}(1-p)^{n-k}$
Use 2ND VARS, binomcdf to evaluate the cumulative probability of at most $k$ occurrences out of $n$ independent trials of an event with probability $p$.

1. Select 2ND VARS (i.e. DISTR)
2. Choose B:binomcdf (use the down arrow).
3. Let trials be $n$.
4. Let p be $p$
5. Let x value be $k$.
6. Select Paste and hit ENTER.

TI-83: Do steps 1-2, then enter the values for $n$, $p$, and $k$ separated by commas as follows: binomcdf (n, p, k). Then hit ENTER.

## Practice exercises

Find the number of ways of arranging 3 blue marbles and 2 red marbles. ${ }^{8}$

[^3](G)

There are 13 marbles in a bag. 4 are blue and 9 are red. Randomly draw 5 marbles with replacement. Find the probability you get exactly 3 blue marbles. ${ }^{9}$

## GUIDED PRACTICE 0.11

(G)

There are 13 marbles in a bag. 4 are blue and 9 are red. Randomly draw 5 marbles with replacement. Find the probability you get at most 3 blue marbles (i.e. less than or equal to 3 blue marbles). ${ }^{10}$

[^4]
## Inference for categorical data

## 1-proportion Z-interval and Z-test

O०. TI-83/84: 1-PROPORTION Z-INTERVAL
Use STAT, TESTS, 1-PropZInt.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose $A: 1$-PropZInt.
4. Let x be the number of yes's (must be an integer).
5 . Let n be the sample size.
5. Let C -Level be the desired confidence level.
6. Choose Calculate and hit ENTER, which returns
(__,__) the confidence interval
$\hat{p} \quad$ the sample proportion
$n$ the sample size

ㅇ․ TI-83/84: 1-PROPORTION Z-TEST
Use STAT, TESTS, 1-PropZTest.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose 5:1-PropZTest.
4. Let $p_{0}$ be the null or hypothesized value of $p$.
5. Let x be the number of yes's (must be an integer).
6. Let $n$ be the sample size.
7. Choose $\neq,<$, or $>$ to correspond to $\mathrm{H}_{A}$.
8. Choose Calculate and hit ENTER, which returns
z Z-statistic
p p-value
$\hat{p}$ the sample proportion
n the sample size

## Practice exercises

## GUIDED PRACTICE 0.12

Using a calculator, evaluate the confidence interval from the example on intelligent life. Recall that we wanted to find a $95 \%$ confidence interval for the proportion of U.S. adults who think there is intelligent life on other planets. The sample percent was $68 \%$ and the sample size was $1,033 .{ }^{11}$

## GUIDED PRACTICE 0.13

Using a calculator, find the test statistic and p-value for the example on nuclear energy. Recall that we were looking for evidence that more than half of U.S. adults oppose nuclear energy. The sample percent was $54 \%$, and the sample size was 1019. ${ }^{12}$

[^5]
## 2-proportion Z-interval and Z-test

## 윽 TI-83/84: 2-PROPORTION Z-INTERVAL

Use STAT, TESTS, 2-PropZInt.

1. Choose Stat.
2. Right arrow to TESTS.
3. Down arrow and choose B:2-PropZInt.
4. Let x 1 be the number of yes's (must be an integer) in sample 1 and let n 1 be the size of sample 1 .
5. Let x 2 be the number of yes's (must be an integer) in sample 2 and let n 2 be the size of sample 2 .
6. Let C-Level be the desired confidence level.
7. Choose Calculate and hit ENTER, which returns:
(_, _) the confidence interval
$\hat{p}_{1} \quad$ sample 1 proportion $\quad n_{1} \quad$ size of sample 1
$\hat{p}_{2} \quad$ sample 2 proportion $\quad n_{2} \quad$ size of sample 2

은 TI-83/84: 2-PROPORTION Z-TEST
Use STAT, TESTS, 2-PropZTest.

1. Choose Stat.
2. Right arrow to TESTS.
3. Down arrow and choose $6: 2$-PropZTest.
4. Let x 1 be the number of yes's (must be an integer) in sample 1 and let n 1 be the size of sample 1 .
5. Let x 2 be the number of yes's (must be an integer) in sample 2 and let n 2 be the size of sample 2 .
6. Choose $\neq,<$, or $>$ to correspond to $\mathrm{H}_{A}$.
7. Choose Calculate and hit ENTER, which returns:
z Z-statistic $\quad p \quad p$-value
$\hat{\mathrm{p}}_{1}$ sample 1 proportion $\hat{\mathrm{p}}$ pooled sample proportion
$\hat{\mathrm{p}}_{2}$ sample 2 proportion

## Practice exercises

## GUIDED PRACTICE 0.14

A quality control engineer collects a sample of gears, examining 1000 gears from each company and finds that 879 gears pass inspection from the current supplier and 958 pass inspection from the prospective supplier. Use a calculator to find a $95 \%$ confidence interval for the difference (current - prospective) in the proportion that would pass inspection. ${ }^{13}$

## GUIDED PRACTICE 0.15

Use a calculator to find the test statistic, p-value, and pooled proportion for a test with: $H_{A}: p$ for fish oil $<p$ for placebo. ${ }^{14}$

|  | heart attack | no event | Total |
| :--- | :---: | :---: | :---: |
| fish oil | 145 | 12788 | 12933 |
| placebo | 200 | 12738 | 12938 |

[^6]
## Finding areas under the chi-square curve

## TI-84: FINDING AN UPPER TAIL AREA UNDER THE CHI-SQUARE CURVE

Use the $\chi^{2} \mathrm{cdf}$ command to find areas under the chi-square curve.

1. Hit 2ND VARS (i.e. DISTR).
2. Choose $8: \chi^{2}$ cdf.
3. Enter the lower bound, which is generally the chi-square value.
4. Enter the upper bound. Use a large number, such as 1000.
5. Enter the degrees of freedom.
6. Choose Paste and hit Enter.

TI-83: Do steps 1-2, then type the lower bound, upper bound, and degrees of freedom separated by commas. e.g. $\chi^{2} \operatorname{cdf}(5,1000,3)$, and hit ENTER.

## Chi-square goodness of fit test

․ TI-84: CHI-SQUARE GOODNESS OF FIT TEST
Use STAT, TESTS, $\chi^{2}$ GOF-Test.

1. Enter the observed counts into list L1 and the expected counts into list L2.
2. Choose Stat.
3. Right arrow to TESTS.
4. Down arrow and choose $\mathrm{D}: \chi^{2} \mathrm{GOF}-$ Test.
5. Leave Observed: L1 and Expected: L2.
6. Enter the degrees of freedom after df:
7. Choose Calculate and hit ENTER, which returns:
$\chi^{2}$ chi-square test statistic
p p-value
df degrees of freedom
TI-83: Unfortunately the TI-83 does not have this test built in. To carry out the test manually, make list L3 $=(\mathrm{L} 1-\mathrm{L} 2)^{2} / \mathrm{L} 2$ and do 1 -Var-Stats on L3. The sum of L3 will correspond to the value of $\chi^{2}$ for this test.

## Chi-square test for two-way tables

우 TI-83/84: ENTERING DATA INTO A TWO-WAY TABLE

1. Hit $2 \mathrm{ND} \mathrm{x}^{-1}$ (i.e. MATRIX).
2. Right arrow to EDIT.
3. Hit 1 or ENTER to select matrix A.
4. Enter the dimensions by typing \#rows, ENTER, \#columns, ENTER.
5. Enter the data from the two-way table.

## 으 TI-83/84: CHI-SQUARE TEST OF HOMOGENEITY AND INDEPENDENCE

Use STAT, TESTS, $\chi^{2}-$ Test.

1. First enter two-way table data as described in the previous box.
2. Choose Stat.
3. Right arrow to TESTS.
4. Down arrow and choose C: $\chi^{2}-$ Test.
5. Down arrow, choose Calculate, and hit ENTER, which returns

$$
\begin{array}{ll}
\chi^{2} & \text { chi-square test statistic } \\
p & p \text {-value } \\
\text { df } & \text { degrees of freedom }
\end{array}
$$

## TI-83/84: FINDING THE EXPECTED COUNTS

1. First enter two-way table data as described previously.
2. Carry out the chi-square test of homogeneity or independence as described in previous box.
3. Hit $2 N D x^{-1}$ (i.e. MATRIX).
4. Right arrow to EDIT.
5. Hit 2 to see matrix B.

This matrix contains the expected counts.

## Practice exercises

## GUIDED PRACTICE 0.16

Use a calculator to find the upper tail area for the the chi-square distribution with 5 degrees of freedom and a $\chi^{2}=5.1 .{ }^{13}$

## GUIDED PRACTICE 0.17

Use the table below and a calculator to find the $\chi^{2}$-statistic and p -value for chi-square goodness of fit test. ${ }^{16}$

|  | Blue | Orange | Green | Yellow | Red | Brown |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| observed counts: | 133 | 133 | 139 | 103 | 108 | 96 |
| expected counts: | 170.9 | 142.4 | 113.9 | 99.6 | 92.6 | 92.6 |

## GUIDED PRACTICE 0.18

The table below shows approval numbers, based on a random sample conducted by the Pew Research poll. Use a calculator to find the expected values and the $\chi^{2}$-statistic, $d f$, and p -value for the chi-square test for independence. ${ }^{17}$

|  |  | Congress |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Obama | Democrats | Republicans | Total |
| Approve | 842 | 736 | 541 | 2119 |
| Disapprove | 616 | 646 | 842 | 2104 |
| Total | 1458 | 1382 | 1383 | 4223 |

[^7]
## Inference for numerical data

## 1-sample $t$-test and $t$-interval

## ㅇ․ TI-83/84: 1-SAMPLE T-TEST

Use STAT, TESTS, T-Test.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose $2: T-T e s t$.
4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.
5. Let $\mu_{0}$ be the null or hypothesized value of $\mu$.

- If you choose Data, let List be L1 or the list in which you entered your data (don't forget to enter the data!) and let Freq be 1.
- If you choose Stats, enter the mean, SD , and sample size.

6. Choose $\neq,<$, or $>$ to correspond to $\mathrm{H}_{A}$.
7. Choose Calculate and hit ENTER, which returns:
$t \quad t$ statistic $S x$ the sample standard deviation
$p$ p-value $n$ the sample size
$\overline{\mathrm{x}}$ the sample mean

O०, TI-83/84: 1-SAMPLE T-INTERVAL
Use STAT, TESTS, TInterval.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose 8:TInterval.
4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.

- If you choose Data, let List be L1 or the list in which you entered your data (don't forget to enter the data!) and let Freq be 1.
- If you choose Stats, enter the mean, SD , and sample size.

5. Let C -Level be the desired confidence level.
6. Choose Calculate and hit ENTER, which returns:
(__,__) the confidence interval
$\overline{\mathrm{x}} \quad$ the sample mean
Sx the sample SD
n
the sample size

## Practice exercises

## GUIDED PRACTICE 0.19

The average time for all runners who finished the Cherry Blossom Run in 2006 was 93.3 minutes. In 2017, the average time for 100 randomly selected participants was 97.3 , with a standard deviation of 17.0 minutes. Use a calculator to find the $T$-statistic and p-value for the appropriate test to see if the average time for the participants in 2017 is different than it was in $2006 .{ }^{18}$

## GUIDED PRACTICE 0.20

Use a calculator to find a $95 \%$ confidence interval for the mean mercury content in croaker white fish (Pacific). The sample size was 15 , and the sample mean and standard deviation were computed as 0.287 and 0.069 ppm (parts per million), respectively. ${ }^{19}$

[^8]
## 1-sample $t$-test and $t$-interval with paired data

## TI-83/84: 1-SAMPLE T-TEST WITH PAIRED DATA

Use STAT, TESTS, T-Test.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose $2: T-T e s t$.
4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.
5. Let $\mu_{0}$ be the null or hypothesized value of $\mu_{d i f f}$.

- If you choose Data, let List be L3 or the list in which you entered the differences (don't forget to enter the differences!) and let Freq be 1.
- If you choose Stats, enter the mean, SD, and sample size of the differences.

6. Choose $\neq,<$, or $>$ to correspond to $\mathrm{H}_{A}$.
7. Choose Calculate and hit ENTER, which returns: t t statistic
p p-value
$\overline{\mathrm{x}} \quad$ the sample mean of the differences
Sx the sample SD of the differences
n the sample size of the differences

## TI-83/84: 1-SAMPLE T-INTERVAL WITH PAIRED DATA

Use STAT, TESTS, TInterval.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose 8:TInterval.
4. Choose Data if you have all the data or Stats if you have the mean and standard deviation.

- If you choose Data, let List be L3 or the list in which you entered the differences (don't forget to enter the differences!) and let Freq be 1.
- If you choose Stats, enter the mean, SD, and sample size of the differences.

5. Let C-Level be the desired confidence level.
6. Choose Calculate and hit ENTER, which returns:
(__,_) the confidence interval for the mean of the differences
$\overline{\mathrm{x}} \quad$ the sample mean of the differences
Sx the sample SD of the differences
$n$ the number of differences in the sample

## Practice exercises

## GUIDED PRACTICE 0.21

In our UCLA textbook example, we had 68 paired differences. Because $d f=67$ was not on our $t$-table, we rounded the $d f$ down to 60 . This gave us a $95 \%$ confidence interval ( $0.325,6.834$ ). Use a calculator to find the more exact $95 \%$ confidence interval based on 67 degrees of freedom. How different is it from the one we calculated based on 60 degrees of freedom? ${ }^{20}$

| $n_{\text {diff }}$ | $\bar{x}_{\text {diff }}$ | $s_{\text {diff }}$ |
| :---: | :---: | :---: |
| 68 | 3.58 | 13.42 |

## GUIDED PRACTICE 0.22

Use the data in the table above to find the test statistic and p-value for a test of $H_{0}: \mu_{\text {diff }}=0$ versus $H_{A}: \mu_{\text {diff }} \neq 0 .{ }^{21}$

[^9]
## 2-sample $t$-test and $t$-interval

## 은 TI-83/84: 2-SAMPLE T-TEST

Use STAT, TESTS, 2 -SampTTest.

1. Choose Stat.
2. Right arrow to TESTS.
3. Choose 4:2-SampTTest.
4. Choose Data if you have all the data or Stats if you have the means and standard deviations.

- If you choose Data, let List1 be L1 or the list that contains sample 1 and let List2 be L2 or the list that contains sample 2 (don't forget to enter the data!). Let Freq1 and Freq2 be 1.
- If you choose Stats, enter the mean, SD, and sample size for sample 1 and for sample 2

5. Choose $\neq,<$, or $>$ to correspond to $\mathrm{H}_{A}$.
6. Let Pooled be No.
7. Choose Calculate and hit ENTER, which returns:

| t | t statistic | Sx 1 | SD of sample 1 |
| :--- | :--- | :--- | :--- |
| p | p-value | Sx 2 | SD of sample 2 |
| df | degrees of freedom | n 1 | size of sample 1 |
| $\overline{\mathrm{X}}_{1}$ | mean of sample 1 | n 2 | size of sample 2 |
| $\overline{\mathrm{X}}_{2}$ | mean of sample 2 |  |  |

O०, TI-83/84: 2-SAMPLE T-INTERVAL
Use STAT, TESTS, 2-SampTInt.

1. Choose Stat.
2. Right arrow to TESTS.
3. Down arrow and choose $0: 2$-SampTTInt.
4. Choose Data if you have all the data or Stats if you have the means and standard deviations.

- If you choose Data, let List1 be L1 or the list that contains sample 1 and let List2 be L2 or the list that contains sample 2 (don't forget to enter the data!). Let Freq1 and Freq2 be 1.
- If you choose Stats, enter the mean, SD, and sample size for sample 1 and for sample 2.

5. Let C-Level be the desired confidence level and let Pooled be No.
6. Choose Calculate and hit ENTER, which returns:

| $(\ldots,-\quad)$ | the confidence interval | Sx1 | SD of sample 1 |
| :--- | :--- | :--- | :--- |
| df | degrees of freedom | Sx2 | SD of sample 2 |
| $\overline{\mathrm{x}}_{1}$ | mean of sample 1 | n1 | size of sample 1 |
| $\overline{\mathrm{x}}_{2}$ | mean of sample 2 | n2 | size of sample 2 |

## Practice exercises

## GUIDED PRACTICE 0.23

Use the data below and a calculator to find the test statistics and p-value for a one-sided test, testing whether there is evidence that embryonic stem cells (ESCs) help improve heart function for sheep that have experienced a heart attack. ${ }^{22}$

|  | $n$ | $\bar{x}$ | $s$ |
| :--- | ---: | ---: | ---: |
| ESCs | 9 | 3.50 | 5.17 |
| control | 9 | -4.33 | 2.76 |

## GUIDED PRACTICE 0.24

Use the data below and a calculator to find a $95 \%$ confidence interval for the difference in average scores between Version A and Version B of the exam from the previous example. ${ }^{23}$

| Version | $n$ | $\bar{x}$ | $s$ | $\min$ | $\max$ |
| :--- | ---: | ---: | ---: | ---: | ---: |
| A | 30 | 79.4 | 14 | 45 | 100 |
| B | 30 | 74.1 | 20 | 32 | 100 |

[^10]
## Introduction to linear regression

Finding $a, b, R^{2}$, and $r$ for a linear model

ㅇ․ TI-84: FINDING $a, b, R^{2}$, AND $r$ FOR A LINEAR MODEL
Use STAT, CALC, LinReg ( $\mathrm{a}+\mathrm{bx}$ ).

1. Choose Stat.
2. Right arrow to CALC.
3. Down arrow and choose 8:LinReg ( $a+b x$ ).

- Caution: choosing 4:LinReg $(\mathrm{ax}+\mathrm{b})$ will reverse $a$ and $b$.

4. Let Xlist be L1 and Ylist be L2 (don't forget to enter the $x$ and $y$ values in L1 and L2 before doing this calculation).
5. Leave FreqList blank.
6. Leave Store RegEQ blank.
7. Choose Calculate and hit ENTER, which returns:
a $\quad a$, the y -intercept of the best fit line
$\mathrm{b} \quad b$, the slope of the best fit line
$r^{2} \quad R^{2}$, the explained variance
$r \quad r$, the correlation coefficient
TI-83: Do steps 1-3, then enter the $x$ list and $y$ list separated by a comma, e.g. LinReg ( $\mathrm{a}+\mathrm{bx}$ ) L1, L2, then hit ENTER.

## What to do if $r^{2}$ and $r$ do not show up on a TI-83/84

WHAT TO DO IF $r^{2}$ AND $r$ DO NOT SHOW UP ON A TI-83/84
If $r^{2}$ and $r$ do now show up when doing STAT, CALC, LinReg, the diagnostics must be turned on. This only needs to be once and the diagnostics will remain on.

1. Hit 2ND 0 (i.e. CATALOG).
2. Scroll down until the arrow points at DiagnosticOn.
3. Hit ENTER and ENTER again. The screen should now say:

Diagnostic0n
Done

## What to do if a TI-83/84 returns: ERR: DIM MISMATCH

## WHAT TO DO IF A TI-83/84 RETURNS: ERR: DIM MISMATCH

This error means that the lists, generally L1 and L2, do not have the same length.

1. Choose 1: Quit.
2. Choose STAT, Edit and make sure that the lists have the same number of entries.

## Practice exercises

## GUIDED PRACTICE 0.25

The data set loan50, introduced in Chapter 1, contains information on randomly sampled loans offered through the Lending Club. A subset of the data matrix is shown in Figure 1. Use a calculator to find the equation of the least squares regression line for predicting loan amount from total income. ${ }^{24}$

|  | total_income | loan_amount |
| :--- | ---: | ---: |
| 1 | 59000 | 22000 |
| 2 | 60000 | 6000 |
| 3 | 75000 | 25000 |
| 4 | 75000 | 6000 |
| 5 | 254000 | 25000 |
| 6 | 67000 | 6400 |
| 7 | 28800 | 3000 |

Figure 1: Sample of data from loan50.

[^11]
## $t$-test and $t$-interval for the slope of a regression line

## TI-83/84: T-TEST FOR THE SLOPE OF A REGRESSION LINE

Use STAT, TESTS, LinRegTTest.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose F:LinRegTest. (On TI-83 it is E:LinRegTTest).
4. Let Xlist be L1 and Ylist be L2. (Don't forget to enter the $x$ and $y$ values in L1 and L2 before doing this test.)
5. Let Freq be 1.
6. Choose $\neq,<$, or $>$ to correspond to $\mathrm{H}_{A}$.
7. Leave RegEQ blank.
8. Choose Calculate and hit ENTER, which returns:

| t | t statistic | b | $b$, slope of the line |
| :--- | :--- | :--- | :--- |
| p | p -value | s | st. dev. of the residuals |
| df | degrees of freedom for the test | $\mathrm{r}^{2}$ | $R^{2}$, explained variance |
| a | $a$, y-intercept of the line | r | $r$, correlation coefficient |

TI-84: T-INTERVAL FOR THE SLOPE OF A REGRESSION LINE
Use STAT, TESTS, LinRegTInt.

1. Choose STAT.
2. Right arrow to TESTS.
3. Down arrow and choose $G$ : LinRegTest.

- This test is not built into the TI-83.

4. Let Xlist be L1 and Ylist be L2. (Don't forget to enter the $x$ and $y$ values in L1 and L2 before doing this interval.)
5. Let Freq be 1.
6. Enter the desired confidence level.
7. Leave RegEQ blank.
8. Choose Calculate and hit ENTER, which returns:
(__,_) the confidence interval
b $\quad b$, the slope of best fit line of the sample data
df degrees of freedom associated with this confidence interval
s standard deviation of the residuals
a $\quad a$, the y -intercept of the best fit line of the sample data
$r^{2} \quad R^{2}$, the explained variance
$r \quad r$, the correlation coefficient

[^0]:    ${ }^{1}$ The summary statistics should be $\overline{\mathrm{x}}=9.1, \mathrm{Sx}=7.475, \mathrm{Q} 1=3$, etc. The box plot should be as follows.

[^1]:    ${ }^{2}$ normalcdf gives the result without drawing the graph. To draw the graph, do 2nd VARS, DRAW, 1:ShadeNorm. However, beware of errors caused by other plots that might interfere with this plot.
    ${ }^{3}$ Now we want to shade to the right. Therefore our lower bound will be 2 and the upper bound will be 5 (or a number bigger than 5 ) to get $P(Z>2)=0.023$.

[^2]:    ${ }^{4}$ Here we are given both the lower and the upper bound. Lower bound is -1.5 and upper bound is 1.5 . The area under the normal curve between -1.5 and $1.5=P(-1.5<Z<1.5)=0.866$.
    ${ }^{5}$ If $20 \%$ of the area is the right, then $80 \%$ of the area is to the left. Letting area be 0.80 , we get $Z=0.841$.
    ${ }^{6}$ www.biomedcentral.com/1471-2393/8/5
    ${ }^{7} Z=\frac{10-7.44}{1.33}=1.925$. Using a lower bound of 2 and an upper bound of 5 , we get $P(Z>1.925)=0.027$. Approximately $2.7 \%$ of the newborns weighed over 10 pounds.

[^3]:    ${ }^{8}$ Here $n=5$ and $k=3$. Doing 5 nCr 3 gives the number of combinations as 10 .

[^4]:    ${ }^{9}$ Here, $n=5, p=4 / 13$, and $k=3$, so set trials $=5, \mathrm{p}=4 / 13$ and x value $=3$. The probability is 0.1396 .
    ${ }^{10}$ Similarly, set trials $=5, p=4 / 13$ and x value $=3$. The cumulative probability is 0.9662 .

[^5]:    ${ }^{11}$ Navigate to 1-PropZInt on the calculator. To find $x$, the number of yes responses in the sample, we multiply the sample proportion by the sample size. Here $0.68 \times 1033=702.44$. We must round this to an integer, so we use $\mathrm{x}=702$. Also, $\mathrm{n}=1033$ and C -Level $=0.95$. The $95 \%$ confidence interval is ( 0.651 , 0.708)
    ${ }^{12}$ Navigate to 1 -PropZTest on the calculator. Let $p_{0}=0.5$. To find x , do $0.54 \times 1019=550.26$. This needs to be an integer, so round to the closest integer. Here $\mathrm{x}=550$. Also, $\mathrm{n}=1019$. We are looking for evidence that greater than half oppose, so choose $>$ po. When we do Calculate, we get the test statistic: $Z=2.64$ and the $p$-value: $p=0.006$.

[^6]:    ${ }^{13}$ Navigate to 2-PropZInt on the calculator. Let $\mathrm{x} 1=879, \mathrm{n} 1=1000, \mathrm{x} 2=958$, and $\mathrm{n} 2=1000$. C-Level is .95 . This should lead to an interval of $(-0.1027,-0.0553)$, which matches what we found previously.
    ${ }^{14}$ Navigate to 2-PropZTest on the calculator. Correctly going through the calculator steps should lead to a solution with the test statistic $z=-2.977$ and the $p$-value $p=0.00145$. These two values match our calculated values from the previous example to within rounding error. The pooled proportion is given as $\hat{p}=0.0133$. Note: values for x 1 and x 2 were given in the table. If, instead, proportions are given, find x 1 and $\times 2$ by multiplying the proportions by the sample sizes and rounding the result to an integer.

[^7]:    ${ }^{15}$ Use a lower bound of 5.1 , an upper bound of 1000 , and $d f=5$. The upper tail area is 0.4038 .
    ${ }^{16}$ Enter the observed counts into L1 and the expected counts into L2. the GOF test. Make sure that Observed: is L1 and Expected: is L2. Let df: be 5. You should find that $\chi^{2}=17.36$ and p-value $=0.004$.
    ${ }^{17}$ First create a $2 \times 3$ matrix with the data. The final summaries should be $\chi^{2}=106.4$, p -value is $p=8.06 \times 10^{-24} \approx 0$, and $\mathrm{df}=2$. Below is the matrix of expected values:

    |  | Obama | Congr. Dem. | Congr. Rep. |
    | :--- | :---: | :---: | :---: |
    | Approve | 731.59 | 693.45 | 693.96 |
    | Disapprove | 726.41 | 688.55 | 689.04 |

[^8]:    ${ }^{18}$ Navigate to T-Test. Let $\mu_{0}$ be 93.3. $\overline{\mathrm{x}}$ is $97.3, \mathrm{~S}_{\mathrm{x}}$ is 17.0 , and $\mathrm{n}=100$. Choose $\neq$ to correspond to $H_{A}$. We get $\mathrm{t}=2.353$ and the p -value $\mathrm{p}=0.021$. The $d f=100-1=99$.
    ${ }^{19}$ Navigate to TInterval. We do not have all the data, so choose Stats. Enter $\overline{\mathrm{x}}$ and Sx. Note: Sx is the sample standard deviation (0.069), not the $S E$ of the sample mean. Let $\mathrm{n}=15$ and C-Level $=0.95$. This should give the interval $(0.249,0.325)$. The $d f=15-1=14$

[^9]:    ${ }^{20}$ Navigate to TInterval. We do not have all the data, so choose Stats. Enter $\bar{x}=3.58$ and $\mathrm{Sx}=13.42$. Let $\mathrm{n}=68$ and C-Level $=0.95$. This should give the interval ( $0.332,6.828$ ). The intervals are equivalent when rounded to two decimal places.
    ${ }^{21}$ Navigate to T-Test. We do not have all the data, so choose Stats. Enter $\mu_{0}=0, \overline{\mathrm{x}}=3.58, \mathrm{Sx}=$ $13.42, \mathrm{n}=68$, and choose $\neq \mu_{0}$ since the alternative hypothesis is two-sided. This should give the interval $\mathrm{t}=2.2$ and $\mathrm{p}=0.031$.

[^10]:    ${ }^{22}$ Navigate to 2 -SampTTest. Because we have the summary statistics rather than all of the data, choose Stats. Let $\overline{\mathrm{x}} 1=3.50, \mathrm{Sx} 1=5.17, \mathrm{n} 1=9, \overline{\mathrm{x}} 2=-4.33, \mathrm{Sx} 2=2.76$, and $\mathrm{n} 2=9$. We get $\mathrm{t}=4.01$, and the p -value $p=8.4 \times 10^{-} 4=0.00084$. The degrees of freedom for the test is $d f=12.2$.
    ${ }^{23}$ Navigate to 2 -SampTInt. Because we have the summary statistics rather than all of the data, choose Stats. Let $\overline{\mathrm{x}} 1=79.41, \mathrm{Sx} 1=14, \mathrm{n} 1=30, \overline{\mathrm{x}} 2=74.1, \mathrm{Sx} 2=20$, and $\mathrm{n} 2=30$. The interval is $(-3.6,14.2)$ with $d f=51.9$.

[^11]:    ${ }^{24} \mathrm{a}=11121$ and $\mathrm{b}=0.0043$, therefore $\hat{y}=11121+0.0043 x$.

